

$$f(x) = ae^x - a + 1$$

$$g(x) = ae^x - a + g(0) - 1 + \cos x$$